Kenilworth Public Schools Curriculum Guide

Content Area: Algebra II/Trig Honors

Grade: 11

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by: Mendy Petti

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Class Name: Algebra II/Trig Honors

Grade Level: 10 - 11

August 2023

Unit 1- Quadratic Functions & Factoring	Unit 2- Polynomials and Polynomial Functions	Unit 3- Rational Functions	Unit 4- Rational Exponents and Radical Functions	Unit 5- Exponential and Logarithmic Functions	Unit 6- Sequences and Series, Data Analysis, Right Triangle Trig,	Unit 7- Trigonometry
Weeks 1-6	Weeks 7-12	Weeks 13-17	Weeks 18-21	Weeks 22-27	Weeks 28-32	Weeks 33-38
Unit Description: Graph, analyze, model and solve quadratic functions.	Unit Description: Use properties of exponents. Graph, analyze, model, and solve polynomial functions.	Unit Description: Graph, analyze, model and solve rational functions.	Unit Description: Understand and use rational exponents. Analyze and graph radical functions. Solve radical equations.	Unit Description: Graph, analyze, model, and solve exponential and logarithmic functions.	Unit Description: Define, analyze, and find sums of sequences and series. Apply the fundamentals of data analysis and probability distributions. Apply basic Right Triangle Trigonometry.	Unit Description: Understand and Apply Trigonometric Properties and Identities. Graph trigonometric functions.
Unit Targets:Graph quadratic functions in standard form.	Unit Targets:Use Properties of Exponents.	Unit Targets:Model Inverse and Joint Variation.	Unit Targets:Evaluate nthRoots and use	Unit Targets:Graph exponential growth functions.	Unit Targets:Define and use Sequences and Series.	Unit Targets:Use Trigonometry with Right Triangles.

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 Graph quadratic functions in vertex or intercept form. Solve x²+bx+c=0 by factoring. Solve ax²+bx+c=0 by factoring. Solve quadratic equations by find square roots. Perform Operations with complex numbers. Solve Quadratics by completing the square. Use the Quad. Formula and the discriminant. Graph and Solve Quad. Inequalities. 	 Evaluate and Graph Polynomial Functions. Add, Subtract, and Multiply Polynomials. Factor and Solve Polynomial Equations. Apply the Remainder and Factor Theorems. Find Rational Zeros. Apply the Fundamental Theorem of Algebra. Analyze Graphs of Polynomial Functions. 	 Graph Simple Rational Functions. Graph General Rational Functions. Multiply and Divide Rational Expressions. Add and Subtract Rational Expressions. Solve Rational Equations. Describe and Compare Function Characteristics. 	Rational Exponents. • Apply Properties of Rational Exponents. • Perform Function Operations and Composition. • Use Inverse Functions. • Graph Square Root and Cube Root Functions. • Solve Radical Equations.	 Graph exponential decay functions. Use functions involving e. Evaluate logarithms and graph logarithmic functions. Apply properties of logarithms. Solve exponential and logarithmic equations. Create and apply exponential and power functions. 	 Analyze arithmetic sequences and series. Analyze geometric sequences and series. Evaluate Sums of infinite geometric series. Analyze variation. Construct and interpret Normal Distributions. 	 Define the Unit Circle, and General Angles and Use Radian Measure. Derive the unit circle using right triangle trig.** Evaluate Trig Functions of any angle. Evaluate Inverse Trig Functions. Apply the Laws of Sines and Cosines. Graph, translate and reflect Trig Functions. Verify Trig Identities. Solve Trig Equations. Write Trig Functions and Models. Apply Sum and Difference Formulas. Apply Multiple-Angle Formulas.
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ALGEBRA II TRIG HONORS

Grades 10-12 August 2023

Unit 1: Quadratic Functions and Factoring

Unit summary: Graph, analyze, model and solve quadratic functions.

Primary interdisciplinary connections: Business, Social Studies, Science

21st **Century Themes:** Global Awareness, Financial, Economic, Business and Entrepreneurial Literacy, Life and Career Skills, Information Literacy

Learning Targets

Standards: NJSLS: 9-12.F.IF.7a, 9-12.A.SSE.3a, 9-12.A.REI.4b, 9-12.N.CN.2, 9-12.A.REI.4a, 9-12.N.CN.7

Content Statements:

- 1 Quadratic functions in standard form
- 2 Quadratic functions in vertex or intercept form
- 3 Factoring $x^2+bx+c=0$
- 4 Factoring $ax^2+bx+c=0$
- 5 | Square roots of Quadratic Equations
- 6 | Complex numbers
- 7 | Completing the square
- 8 The Quadratic Formula and the discriminant
- 9 Quadratic Inequalities

Big Idea: Many real-life situations can be modeled using quadratic functions.

Unit Essential Questions:

- What is the shape and characteristics of the graph of a quadratic function?
- What real-world situations can be modeled by quadratics?
- How can quadratic functions be solved and how many solutions can exist?

Unit Enduring Understandings:

- Quadratic functions are in the shape of a parabola.
- There are as many as two solutions for a quadratic function and a variety of techniques for finding them.

Unit Learning Targets

Students will...

- Graph quadratic functions in standard form.
- Graph quadratic functions in vertex or intercept form.
- Solve $x^2+bx+c=0$ by factoring.
- Solve $ax^2+bx+c=0$ by factoring.
- Solve quadratic equations by finding square roots.
- Perform Operations with complex numbers.
- Solve Quadratics by completing the square.
- Use the Quadratic Formula and the discriminant.
- Graph and Solve Quadratic Inequalities.

Evidence of Learning

Summative Assessment: Quizzes, Tests

- Homework
- Classwork
- Other activities at teacher's discretion

Lesson Plans	
Activities	Timeframe
 Graph the parent function for quadratic functions, identify the characteristics of the graph, and explore the effects of changing the coefficients of quadratic functions in standard form. Graph the parent function. Identify the vertex and axis of symmetry. Explore the effect of changing the coefficient "a" to values greater than and less than one and to positive and negative values. Explore the effect of adding a "c" coefficient and changing its value. Explore the effect of adding a "b" coefficient and changing its value. 	Weeks 1-12
 identify the characteristics of the graph, and explore the effects of changing the coefficients of quadratic functions in standard form. 1. Graph the parent function. 2. Identify the vertex and axis of symmetry. 3. Explore the effect of changing the coefficient "a" to values greater than and less than one and to positive and negative values. 4. Explore the effect of adding a "c" coefficient and changing its value. 5. Explore the effect of adding a "b" coefficient 	Weeks 1-12

- 6. Recognize that "c" is the y-intercept and discuss the formula for the x-coordinate of the vertex.
- Model dropped objects with the quadratic function.
 - 1. Given the model function, calculate times for objects to fall to earth from various heights. Discuss the relationship between the height and the time to drop to the earth. Demonstrate with actual objects. Discuss that mass does not affect the time to drop (assuming negligible air resistance).
 - Extend the discussion to include the path of all objects in flight, such as that of a batted baseball.
 Discuss the independence of horizontal and vertical motion.
 - 3. Find maximum heights of objects in flight.

Teacher Resources	Teacher Note
 Graphing software projected on a large screen Actual objects of various weights to drop as demonstrations Blackboard or whiteboard 	If all students are provided graphing calculators, add an individual practice exercise to the first activity.

Unit 2: Polynomials and Polynomial Functions

Unit summary: Use properties of exponents. Graph, analyze, model, and solve polynomial functions.

Primary interdisciplinary connections: Business, Social Studies, Science

21st **Century Themes:** Global Awareness, Financial, Economic, Business and Entrepreneurial Literacy, Life and Career Skills, Information Literacy

Learning Targets

Standards: NJSLS: 9-12.N.RN.1, 9-12.F.IF.7c, 9-12. A.APR.1, 9-12.A.SSE.2, 9-12.A.APR.2, 9-12.N.CN.9

Content Statements:

1 | Properties of Exponents

Evaluate and Graph Polynomial Functions
Add, Subtract, and Multiply Polynomials
Polynomial Equations
Remainder and Factor Theorems
Rational Zeros
Fundamental Theorem of Algebra
Analyze Graphs Polynomial Functions

Big Idea: Perform Operations on Polynomial expressions and graph polynomial functions.

Unit Essential Questions:

- How are addition, subtraction, multiplication, and division applied to polynomials?
- How are polynomials factored?
- What are the shapes and characteristics of the graphs of polynomial functions?

Unit Enduring Understandings:

- Operations can be performed on polynomials.
- Polynomials can be factored using a variety of techniques.
- The number of solutions of polynomial functions is at most the degree.
- The domain is the set of all real numbers and the functions are continuous.

Unit Learning Targets

Students will...

- Use Properties of Exponents.
- Evaluate and Graph Polynomial Functions.
- Add, Subtract, and Multiply Polynomials.
- Factor and Solve Polynomial Equations.
- Apply the Remainder and Factor Theorems.
- Find Rational Zeros.
- Apply the Fundamental Theorem of Algebra.
- Analyze Graphs of Polynomial Functions.

Evidence of Learning

Summative Assessment: Quizzes, Tests

- Homework
- Classwork
- Other activities at teacher's discretion

Lesson Plans	
Activities	Timeframe
 Model volumes of geometric shapes with polynomial functions: Given a rectangle, cylinder, and pyramid, each with dimensions that include variables, find the associated volumes. Include binomials as needed (see pages 92 and 108). Explore the graphs of polynomial functions: Graph a cubic function with a positive leading coefficient and a cubic function with a negative leading coefficient, on the same coordinate plane. Note the characteristics of the graphs. (see page 98 example #5 for possible functions to use) Graph a quartic function with a positive leading coefficient and a quartic function with a negative leading coefficient, on the same coordinate plane. Note the characteristics of the graphs (see page 98 example #5 for possible functions to use). 	Weeks 13-18
3. Summarize the observations. Make conclusions about end behavior (see page 97).	
Teacher Resources	Teacher Note
Graphing software projected onto a large screen	If all students have access to graphing calculators, students may make individual graphs, and make the same observations

Unit 3: Rational Functions

Unit summary: Graph, analyze, model and solve rational functions

Primary interdisciplinary connections: Business, Social Studies, Science

21st **Century Themes:** Global Awareness, Financial, Economic, Business and Entrepreneurial Literacy, Life and Career Skills, Information Literacy

Learning Targets

Standards: NJSLS: 9-12.A.CED.2, 9-12.F.IF.7d, 9-12.A.APR.7, 9-12.A.REI.2, 9-12.F.IF.9

Content Statements:

Inverse and Joint Variation

- 2 Simple Rational Functions3 General Rational Functions
- 3 General Rational Functions
- 4 Multiply and Divide Rational Expressions
- 5 Add and Subtract Rational Expressions
- 6 | Rational Equations
- 7 | Characteristics of Function

Big Idea: Functions with variables in the denominator are defined as rational and can be used to model real-life situations.

Unit Essential Questions:

- What are possible characteristics of the graphs of rational functions?
- What happens when the denominator of a rational expression/function becomes zero?
- How do we solve rational equations?

Unit Enduring Understandings:

- The domain of rational functions may not be the set of all real numbers.
- The graphs of rational functions may contain holes and/or asymptotes.
- There are various ways to solve rational equations.

Unit Learning Targets

Students will...

- Model Inverse and Joint Variation.
- Graph Simple Rational Functions.
- Graph General Rational Functions.
- Multiply and Divide Rational Expressions.
- Add and Subtract Rational Expressions.
- Solve Rational Equations.
- Describe and Compare Function Characteristics.

Evidence of Learning

Summative Assessment: Quizzes, Tests

Formative Assessments:

- Homework
- Classwork
- Other activities at teacher's discretion

Lesson Plans

Activities	Timeframe
 Given that two variables vary inversely, and given one pair of values that satisfy the relationship, write an equation for the function. Repeat this for several different inverse variation functions. Notice a pattern in this process. Given one inverse variation function, one rational function that has a hole in the graph, one rational function that has a single vertical asymptote (not at x=0), and one rational function that has two vertical asymptotes: Discuss values that would not be possible for x. Describe the domain for each function. Display the graphs of each function to illustrate that these values for x indeed cannot exist. 	Weeks 19-24
Teacher Resources	Teacher Note
• Graphing software projected onto a large screen.	If all students have access to graphing calculators, students can graph the functions individually in order make the observations

Unit 4: Rational Exponents and Radical Functions

Unit summary: Understand and use rational exponents. Analyze and graph radical functions. Solve radical equations.

Primary interdisciplinary connections: Business, Social Studies, Science

21st **Century Themes:** Global Awareness, Financial, Economic, Business and Entrepreneurial Literacy, Life and Career Skills, Information Literacy

Learning Targets

Standards: NJSLS: 9-12.N.RN.1, 9-12.N.RN.2, 9-12.F.BF.1, 9-12.F.BF.4, 9-12.F.IF.7b, 9-12.A.REI.2

Content Statements:

- 1 | Roots and Rational Exponents
- 2 | Properties of Rational Exponents
- 3 Function Operations and Composition

- 4 Inverse Functions
- 5 | Square Root and Cube Root Functions
- 6 | Radical Equations

Big Idea: Understand and use rational exponents and graph and solve radical functions.

Unit Essential Questions:

- What are the similarities and differences between rational exponents and radical expressions?
- What are inverse functions and composite functions?
- What are the characteristics of the graphs of square and cube root functions?
- How can radical equations be solved?

Unit Enduring Understandings:

- All radical expressions have an equivalent rational exponent expression.
- Two functions composed in both directions will equal x if and only if the two functions are inverses of each other.
- The graphs of the square and cube root functions have distinct shapes and characteristics.
- Radical equations can be solved by raising each side of the equations to the power of the index.

Unit Learning Targets

Students will...

- Evaluate *n*th Roots and use Rational Exponents.
- Apply Properties of Rational Exponents.
- Perform Function Operations and Composition.
- Use Inverse Functions.
- Graph Square Root and Cube Root Functions.
- Solve Radical Equations.

Evidence of Learning

Summative Assessment: Quizzes, Test

- Homework
- Classwork
- Other activities at teacher's discretion

Lesson Plans			
Activities	Timeframe		

• Simplify given nth roots where n=2, 3, 4 and 5. List perfect squares, perfect cubes, perfect powers of four, and perfect powers of five. Discuss a general procedure	Weeks 25-29
for simplifying roots.	
• Graph the parent function for square roots and explore the characteristics of the graph.	
1. Graph the parent function for square roots	
2. Change the leading coefficient to values that are less than and greater than one. Note the effect on the graph.	
3. Change the leading coefficient to a negative value. Note the effect on the graph.	
4. Add constants that translate the graph. Note the effect on the graph.	
Teacher Resources	Teacher Note
• Graphing software projected onto a large screen	If all students have access to graphing calculators, the graphing can be done individually and the same observations can be made.

Unit 5: Exponential and Logarithmic Functions

Unit summary: Graph, analyze, model, and solve exponential and logarithmic functions.

Primary interdisciplinary connections: Business, Social Studies, Science

21st **Century Themes:** Global Awareness, Financial, Economic, Business and Entrepreneurial Literacy, Life and Career Skills, Information Literacy

Standards: NJSLS: 9-12.F.IF.7e, 9-12.F.BF.5, 9-12.F.LE.4, 9-12.F.LE.2 Content Statements: 1 Exponential growth functions 2 Exponential decay functions 3 Functions involving e 4 Evaluate logarithms and graph logarithmic functions 5 Properties of logarithms 6 Exponential and logarithmic equations 7 Exponential and power functions

Big Idea: Exponential functions can be used to model growth and decay and can be solved using logarithms.

Unit Essential Questions:

- What are the characteristics of the graphs of exponential and logarithmic functions?
- What can be modeled using exponential functions?
- How can operations be performed on exponential and logarithmic functions?
- How can exponential and logarithmic functions be solved?

Unit Enduring Understandings:

- The graphs of exponential functions can be used to model growth and decay.
- There are special properties for performing operations on logarithmic and exponential expressions.
- Exponential and logarithmic functions are inverses and can be used to solve each other.

Unit Learning Targets

Students will...

- Graph exponential growth functions.
- Graph exponential decay functions.
- \bullet Use functions involving e.
- Evaluate logarithms and graph logarithmic functions.
- Apply properties of logarithms.
- Solve exponential and logarithmic equations.
- Create and apply exponential and power functions.

Activities	Timeframe
 Model a family tree with an exponential growth function. 	Weeks 30-24
1. Beginning with oneself, draw a family tree for about four generations.	
Make a table of values for the number of generations, and the corresponding numbers of ancestors.	
3. Explore the pattern. Write a function for the number of ancestors as a function of the generation. Determine the number of ancestors one has going back for a large number of generations.	
 Explore the graphs of exponential decay functions. 1. Graph the parent function for exponential decay functions. 	

Change the value and sign of the leading coefficient. Note the effect on the graph.	
3. Add constants that translate the graph. Note the effect on the graph.	
Teacher Resources	Teacher Note
• Graphing software projected onto large screen	If all students have graphing calculators, the graphs can be made individually and the same changes and observations can be made.

Unit 6: Sequences and Series, Data Analysis, Right Triangle Trig

Unit summary: Define, analyze, and find sums of sequences and series. Apply the fundamentals of data analysis and probability distributions. Apply basic Right Triangle Trigonometry.

Primary interdisciplinary connections: Business, Social Studies, Science

21st **Century Themes:** Global Awareness, Financial, Economic, Business and Entrepreneurial Literacy, Life and Career Skills, Information Literacy

Learning Targets

Standards: NJSLS: 9-12.F.IF.3, 9-12.F.BF.2, 9-12.A.SSE.4, 9-12.A.SSE.3, 9-12.S.ID.4, 9-12.G.SRT.6

Content Statements:

- 1 | Sequences and Series
- 2 | Arithmetic sequences and series
- 3 | Geometric sequences and series
- 4 | Infinite geometric series
- 5 | Variation
- 6 | Normal Distributions

Big Idea: Identifying patterns in sequences and series allows us to create models and make predictions. There are many ways to represent and analyze data via normal distributions. Right triangle trigonometry can be used to calculate missing information about triangle measurements.

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• What is a sequence or a series?

Unit Enduring Understandings:

- What is the difference between arithmetic and geometric sequences/series?
- How does a normal curve model real data?
- How can trigonometry be used to solve triangles representing real-life situations?
- Infinite sequences can be modeled mathematically.
- Understanding the mathematical model of a sequence allows us to find cumulative totals of a series.
- The normal curve can be applied to model numerous real-world scenarios.
- Right triangle trigonometry can be used to solve a triangle given only two measurements.

Unit Learning Targets

Students will...

- Define and use Sequences and Series.
- Analyze arithmetic sequences and series.
- Analyze geometric sequences and series.
- Evaluate Sums of infinite geometric series.
- Analyze variation.
- Construct and interpret Normal Distributions.

Evidence of Learning

Summative Assessment: Quizzes, Test

- Homework
- Classwork
- Other activities at teacher's discretion

Lesson Plans	
Activities	Timeframe
 Investigate an infinite geometric series with the activity on page 459. Calculate the height of tall objects given the angle of inclination to the top of the object from a given distance 	Weeks 35-40
from the base of the object, using right triangle trigonometry. Teacher Resources	Teacher Note

Colored paper, scissors for each student
 Clinometer, measuring tape or measuring wheel
 The trigonometry activity is best done outdoors to calculate the height of very tall objects. As an alternate, it can be accomplished in the classroom and the angle of inclination should be measured from

Unit 7 title: Trigonometry

Unit summary: Understand and Apply Trigonometric Properties and Identities. Graph Trigonometric Functions.

Primary interdisciplinary connections: Business, Social Studies, Science

21st **Century Themes:** Global Awareness, Financial, Economic, Business and Entrepreneurial Literacy, Life and Career Skills, Information Literacy

Learning Targets

Standards: NJSLS: 9-12.F.TF.1, 9-12.F.TF.2, 9-12.F.TF.6, 9-12.G.SRT.11, 9-12.F.IF.7e, 9-12.F.TF.8, 9-12.F.TF.7, 9-12.F.TF.5, 9-12.F.TF.9

Content Statements:

- 1 Right Triangles Trigonometry
- 2 Unit Circle, and General Angles and Use Radian Measure
- 3 Derive the unit circle
- 4 Trigonometric Functions of any angle
- 5 Inverse Trigonometric Functions
- 6 Laws of Sines and Cosines
- 7 Trigonometric Identities
- 8 Trigonometric Equations
- 9 Sum and Difference Formulas
- 10 | Multiply-Angle Formulas

Big Idea: Evaluate trigonometric functions of general angles and apply properties of trigonometric functions. Graph trigonometric functions and define the unit circle.

Unit Essential Questions:

• What are general angles?

Unit Enduring Understandings:

• The unit circle can be used to draw and evaluate trigonometric functions of common angles.

a sitting position.

- How can functions with general angles be evaluated?
- How can operations be performed with trigonometric functions?
- What are the characteristics of the graphs of trigonometric functions?
- Trigonometric properties and identities are used to perform operations on trigonometric expressions and verify identities.
- The trigonometric functions have oscillating graphs and can be used to model real-world cyclical scenarios.

Unit Learning Targets

Students will...

- Use Trigonometry with Right Triangles.
- Define the Unit Circle, and General Angles and Use Radian Measure.
- Derive the unit circle using right triangle trig.
- Evaluate Trig Functions of any angle.
- Evaluate Inverse Trig Functions.
- Apply the Laws of Sines and Cosines.
- Graph, translate and reflect Trig Functions.
- Verify Trig Identities.
- Solve Trig Equations.
- Write Trig Functions and Models.
- Apply Sum and Difference Formulas.
- Apply Multiple- Angle Formulas.

Evidence of Learning

Summative Assessment: Quizzes, Test

- Homework
- Classwork
- Other activities at teacher's discretion

Lesson Plans	
Activities	Timeframe
• Create a unit circle.	40 minutes
 Given a graphic organizer of a circle of radius one with standard angles in degrees, record the corresponding radian measures. 	
2) For each angle, starting at 30 degrees, draw the right triangle using the reference angle, and record	

 the corresponding ordered pair of x and y values at that point on the circle. 3) Repeat step 2 until a pattern is noticed. Complete the ordered pairs for each angle. 4) Explore the sine and cosine values for each angle and note that they are the same as the y and x values of the coordinate pair, respectfully. 	
 Investigate the graphs of the trigonometric functions. 1) In groups, using the unit circles from the activity above, manually graph the sine, cosine, and tangent functions (one function per group), from -360 degrees to +360 degrees. 2) Make observations about the domain and range of each graph. 3) Discuss the period of each graph. Discuss the amplitude of the sine and cosine graphs. 	40 minutes
Teacher Resources	Teacher Note
Unit circle graphic organizerGraph paper	It is preferred that the graphing activity be done on oversized graph paper, if available.